JEE MAIN 2023 Paper with Solution

PHYSICS | 1st Feb 2023 _ Shift-1



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SECTION - A

- A child stands on the edge of the cliff 10 m above the ground and throws a stone horizontally with an 1. initial speed of 5 ms⁻¹. Neglecting the air resistance, the speed with which the stone hits the ground will be ___ ms⁻¹ (given, $g = 10 \text{ ms}^{-2}$).
 - (1)15
- (3)30
- (4)25

Sol. (1)

Along vertical direction

$$u_v = 0$$

$$v_y^2 = u_y^2 + 2a_y g_y$$

$$a_v = +g$$

$$= (0)^2 + 2 \times 10 \times 10$$
$$v_y^2 = 200$$

$$v_v = ?$$

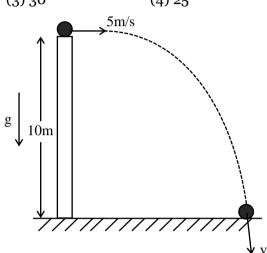
$$v_y^2 = 200$$

$$s_y = 10 \text{ m}$$

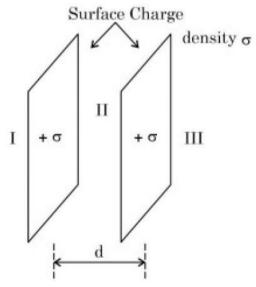
$$v_{y}^{2} = 200$$

$$\therefore \quad v = \sqrt{v_x^2 + v_y^2}$$

$$=\sqrt{25+200} = \sqrt{225}$$



Let σ be the uniform surface charge density of two infinite thin plane sheets shown in figure. Then the 2. electric fields in three different region E_I , E_{II} and E_{III} are:



(1)
$$\vec{E}_I = \frac{2\sigma}{\epsilon_0} \hat{n}, \vec{E}_{II} = 0, \vec{E}_{III} = \frac{2\sigma}{\epsilon_0} \hat{n}$$

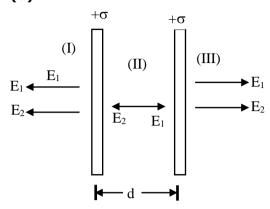
(2)
$$\vec{E}_I = \frac{\sigma}{2\epsilon_0} \hat{n}, \vec{E}_{II} = 0, \vec{E}_{III} = \frac{\sigma}{2\epsilon_0} \hat{n}$$

(3)
$$\vec{E}_I = -\frac{\sigma}{\epsilon_0}\hat{n}, \vec{E}_{II} = 0, \vec{E}_{III} = \frac{\sigma}{\epsilon_0}\hat{n}$$

(4)
$$\vec{E}_I = 0$$
, $\vec{E}_{II} = \frac{\sigma}{\epsilon_0} \hat{n}$, $E_{III} = 0$

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Sol. (3)



$$\therefore \mathbf{E}_{\mathbf{I}} = -\frac{\mathbf{\sigma}}{\mathbf{E}_{\mathbf{0}}} \hat{\mathbf{n}}$$

$$\therefore E_{II} = 0$$

$$\therefore \mathbf{E}_{\text{III}} = -\frac{\sigma}{\mathbf{E}_0} \hat{\mathbf{n}}$$

3. A mercury drop of radius 10^{-3} m is broken into 125 equal size droplets.

Surface tension of mercury is 0.45Nm⁻¹. The gain in surface energy is:

(1)
$$28 \times 10^{-5}$$
 J

(2)
$$17.5 \times 10^{-5}$$
 J

(3)
$$5 \times 10^{-5}$$
 J

(4)
$$2.26 \times 10^{-5}$$
 J

Sol. (4)

[Volume of bigger drop] = [volume of smaller drop] \times 125

$$\frac{4}{3}\pi R^3 = 125 \times \frac{4}{3}\pi r^3$$

$$R^3 = 125r^3$$

$$\therefore R = 5 \times r$$

 \Rightarrow Gain in sinface energy = TdA

$$=0.45\times\left[A_2-A_1\right]$$

$$=0.45\times\left[125\times4\pi r^2-4\pi R^2\right]$$

$$=0.45 \times \left[125 \times 4\pi \left(\frac{R}{5}\right)^2 - 4\pi R^2\right]$$

$$=0.45\times\left[20\pi R^2-4\pi R^2\right]$$

$$=0.45\times16\pi R^{2}$$

$$= 0.45 \times 16 \times 3.14 \times \left(10^{-3}\right)^2$$

$$=2.26\times10^{-5} J$$

4. If earth has a mass nine times and radius twice to that of a planet P. Then $\frac{v_e}{3}\sqrt{x}$ ms⁻¹ will be the minimum velocity required by a rocket to pull out of gravitational force of P, where v_e is escape velocity on earth. The value of x is

(1) 1

- (2)3
- (3)18
- (4)2

$$M_E = 9M_P$$

$$R_E = 2R_P$$

$$\begin{split} V_c^1 &= \sqrt{\frac{2GM_P}{R_P}} = \sqrt{\frac{2G\frac{M_E}{9}}{\frac{R_E}{2}}} \\ &= \sqrt{\frac{2GM_E}{R_E}} \times \sqrt{\frac{2}{9}} \\ \boxed{V_c^1 &= \frac{V_e}{3}\sqrt{2}} \end{split}$$

A sample of gas at temperature *T* is adiabatically expanded to double its volume. The work done by 5. the gas in the process is $\left[\text{given}, \gamma = \frac{3}{2}\right]$:

(1)
$$W = \frac{T}{R} \left[\sqrt{2} - 2 \right]$$

$$(2) W = RT[2 - \sqrt{2}]$$

$$(3) W = TR\left[\sqrt{2} - 2\right]$$

(1)
$$W = \frac{T}{R} \left[\sqrt{2} - 2 \right]$$
 (2) $W = RT \left[2 - \sqrt{2} \right]$ (3) $W = TR \left[\sqrt{2} - 2 \right]$ (4) $W = \frac{R}{T} \left[2 - \sqrt{2} \right]$

Sol.

Work done in the process is given by

$$W = \frac{R}{\gamma - 1}(T_1 - T_2)$$

For adiabatic process:

$$T_{_{1}}V_{_{1}}^{\gamma-1}=T_{_{2}}V_{_{2}}^{\gamma-1}$$

$$TV^{\frac{3}{2}-1} = T_2(2V)^{\frac{3}{2}-1}$$

$$TV^{\frac{1}{2}} = T_2(2V)^{\frac{1}{2}}$$

$$T^2V = T_2^2 \times 2V$$

$$\therefore T_2 = \frac{T}{\sqrt{2}}$$

$$\therefore W = \frac{R}{\gamma - 1} \times \left(T - \frac{T}{\sqrt{2}}\right)$$

$$= 2RT \left[1 - \frac{1}{\sqrt{2}} \right]$$

$$= RT \left[2 - \frac{2}{\sqrt{2}} \right]$$

$$= RT[2-\sqrt{2}]$$

$$W = RT \left[2 - \sqrt{2} \right]$$

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- **6.** $\left(P + \frac{a}{V^2}\right)(V b) = RT$ represents the equation of state of some gases. Where P is the pressure, V is the volume, T is the temperature and a, b, R are the constants. The physical quantity, which has dimensional formula as that of $\frac{b^2}{a}$, will be:
 - (1) Compressibility

(2) Energy density

(3) Modulus of rigidity

(4) Bulk modulus

$$[b] = \lceil L^3 \rceil$$

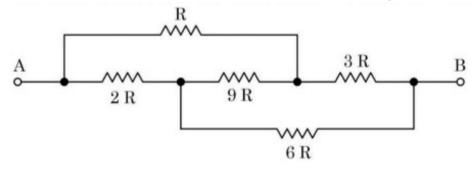
$$[a] = [PV^{2}]$$

$$= [ML^{-1}T^{-2}][L^{6}]$$

$$= [ML^{5}T^{-2}]$$

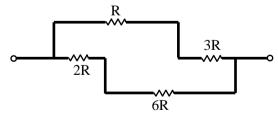
$$\frac{\left[b^{2}\right]}{\left[a\right]} = \frac{\left[L^{6}\right]}{\left\lceil ML^{5}T^{-2}\right\rceil} = \left[M^{-1}L^{1}T^{2}\right]$$

7. The equivalent resistance between *A* and *B* of the network shown in figure:



- $(1)\frac{8}{3}R$
- (2) 21R
- (3)14R
- (4) $11\frac{2}{3}$ R

- Sol. (1
 - ∵ The given network is wheat-stone network



$$\therefore R_{eq} = \frac{4R \times 8R}{4R + 8R}$$
$$= \frac{4R \times 8R}{12R}$$

$$R_{eq} = \frac{8}{3}R$$

8. Match List I with List II:

List I	List II
A. AC generator	I. Presence of both L and C
B. Transformer	II. Electromagnetic Induction
C. Resonance phenomenon to occur	III. Quality factor
D. Sharpness of resonance	IV. Mutual Induction

Choose the correct answer from the options given below:

(1) A-IV, B-III, C-I, D-II

(2) A-IV, B-II, C-I, D-III

(3) A-II, B-IV, C-I, D-III

(4) A-II, B-I, C-III, D-IV

Sol.

- (A) A.C. generator \rightarrow II. Electro-magnetic induction
- (B) transformer \rightarrow IV Mutual induction
- (C) Resonance phenomenon to occur \rightarrow (I) presence of both L and C
- (D) Sharpness of resonance \rightarrow (III) Quality factor

An object moves with speed v_1, v_2 and v_3 along a line segment AB, BC and CD respectively as shown 9. in figure. Where AB = BC and AD = 3AB, then average speed of the object will be:

(1)
$$\frac{(v_1+v_2+v_3)}{3v_1v_2v_3}$$
 (2) $\frac{(v_1+v_2+v_3)}{3}$ (3) $\frac{3v_1v_2v_3}{(v_1v_2+v_2v_3+v_3v_1)}$ (4) $\frac{v_1v_2v_3}{3(v_1v_2+v_2v_3+v_3v_1)}$

$$(1)^{\frac{(v_1+v_2+v_3)}{3v_1v_2v_3}}$$

$$(2)\frac{(v_1+v_2+v_3)}{3}$$

$$(3)\frac{3v_1v_2v_3}{(v_1v_2+v_2v_3+v_3v_1)}$$

$$(4)\frac{v_1v_2v_3}{3(v_1v_2+v_2v_3+v_3v_1)}$$

Sol.

$$= \frac{\text{Total distance}}{\text{Total time}}$$
$$= \frac{3x}{\frac{x}{v_1} + \frac{x}{v_2} + \frac{x}{v_3}}$$

$$= \frac{3}{\left[\frac{1}{v_1} + \frac{1}{v_2} + \frac{1}{v_3}\right]} = \frac{3}{\left[\frac{v_2v_3 + v_1v_3 + v_1v_2}{v_1v_2v_3}\right]}$$

$$\langle v \rangle = \frac{3v_1v_2v_3}{[v_3v_2 + v_1v_2 + v_1v_2]}$$

- 'n' polarizing sheets are arranged such that each makes an angle 45° with the preceding sheet. An unpolarized light of intensity I is incident into this arrangement. The output intensity is found to be I/64. The value of n will be:
 - (1)4
- (2)3
- (3)5
- (4) 6

Sol. (**D**)

According to Malus law:

$$I = \frac{I_0}{2} \left[\cos^2 45 \times \cos^2 45 \times \cos^2 45 \times ...(n-1) \text{ times} \right]$$

$$\frac{\mathbf{I}_0}{64} = \frac{\mathbf{I}_0}{2} \times \left(\frac{1}{2}\right)^{n-1}$$

$$\frac{1}{32} = \frac{1}{2^{n-1}} \Longrightarrow \frac{1}{(2)^5} = \frac{1}{2^{n-1}}$$

$$\therefore n-1=5$$

11. Match List I with List II:

List I	List II
A. Microwaves	I. Radio active decay of the nucleus
B. Gamma rays	II. Rapid acceleration and deceleration of electron in aerials
C. Radio waves	III. Inner shell electrons
D. X-rays	IV. Klystron valve

Choose the correct answer from the options given below:

(1) A-I, B-III, C-IV, D-II

(2) A-IV, B-I, C-II, D-III

(3) A-IV, B-III, C-II, D-I

(4) A-I, B-II, C-III, D-IV

- **Sol.** (B)
 - (A) Micro-wave

(IV) Klystron valve

(B) Gamma rays

(I) Radio-active decay of nucleus

(C) Radio-waves

(II) Rapid acceleration and deceleration of electrons in aerials

(D) X-rays

- (III) Inner shell electron
- **12.** A proton moving with one tenth of velocity of light has a certain de Broglie wavelength of λ . An alpha particle having certain kinetic energy has the same de-Brogle wavelength λ . The ratio of kinetic energy of proton and that of alpha particle is:
 - (1) 2:1
- (2) 1:2
- (3) 1:4
- (4) 4:1

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Sol. (C)

The wavelength of matter is given by

$$\lambda = \frac{h}{p}$$

$$\frac{\lambda_{p}}{\lambda_{\alpha}} = \frac{p_{\alpha}}{p_{p}} = \frac{\sqrt{2k_{\alpha}m_{\alpha}}}{\sqrt{2k_{p}m_{p}}} = 1$$

$$\therefore \frac{k_{\alpha}}{k_{p}} \times \frac{m_{\alpha}}{m_{p}} = 1 \Longrightarrow \frac{k_{\alpha}}{k_{p}} = \frac{m_{p}}{m_{\alpha}}$$

$$\frac{k_{\alpha}}{k_{p}} = \frac{1}{4}$$

A block of mass 5 kg is placed at rest on a table of rough surface. Now, if a force of 30 N is applied in the direction parallel to surface of the table, the block slides through a distance of 50 m in an interval of time 10 s. Coefficient of kinetic friction is (given, $g = 10 \text{ ms}^{-2}$):

Sol. (**D**)

$$S = ut + \frac{1}{2}at^2$$

$$50 = 0 \times t + \frac{1}{2} \times a \times (10)^2$$

$$50 = \frac{1}{2} \times a \times 100$$

$$a = \frac{100}{100} \Longrightarrow \boxed{a = 1 \text{ m/s}^2}$$

$$\sum F_x = ma_x$$

$$30 - \mu mg = ma$$

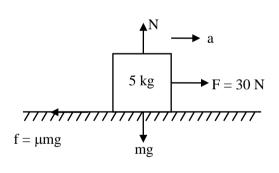
$$30 - \mu \times 50 = 5$$

$$50\mu = 25$$

$$\mu = \frac{25}{50}$$

$$=\frac{1}{2}$$

$$\Rightarrow \mu = 0.5$$



14. Given below are two statements:

Statement I: Acceleration due to gravity is different at different places on the surface of earth.

Statement II: Acceleration due to gravity increases as we go down below the earth's surface. In the light of the above statements, choose the correct answer from the options given below

- (1) Statement I is false but Statement II is true
- (2) Statement I is true but Statement II is false
- (3) Both Statement I and Statement II are false
- (4) Both Statement I and Statement II are true

Sol. (B)

Statement (I) is true But

Statement (II) is false

- **15.** Which of the following frequencies does not belong to FM broadcast.
 - (1) 64MHz
- (2) 89MHz
- (3) 99MHz
- (4) 106MHz

Sol. (A)

The Frequencies for FM Broadcast is between 87.5 MHz to 108 MHz.

- **16.** The mass of proton, neutron and helium nucleus are respectively 1.0073*u*, 1.0087*u* and 4.0015*u*. The binding energy of helium nucleus is:
 - (1) 28.4MeV
- (2) 56.8MeV
- (3) 14.2MeV
- (4) 7.1MeV

Sol. (A)

$$2P + 2n = {}_{2}^{4}He + E$$

$$\therefore$$
 B.E = $[2 \times (1.0073 + 1.0087) - 4.0015] \times 931$

- $= 0.0305 \times 931$
- = 28.3955 MeV
- 17. A steel wire with mass per unit length 7.0×10^{-3} kg m⁻¹ is under tension of 70 N. The speed of transverse waves in the wire will be:
 - (1) 100 m/s
- (2) 10 m/s
- (3) 50 m/s
- (4) $200\pi m/s$

Sol. (A)

The velocity of Transverse wave on string is given by

$$V = \sqrt{\frac{T}{\mu}}$$

$$= \sqrt{\frac{70}{7 \times 10^{-3}}} = \sqrt{\frac{70 \times 10^{3}}{7}}$$

$$= \sqrt{10^{4}} = 100 \text{ m/s}$$

18. Match List I with List II:

List I	List II
A. Intrinsic semiconductor	I. Fermi-level near the valence band
B. n-type semiconductor	II Fermi-level in the middle of valence and conduction band
C. p-type semiconductor	III. Fermi-level near the conduction band
D. Metals	IV. Fermi-level inside the conduction band

Choose the correct answer from the options given below:

(1) A-II, B-III, C-I, D-IV

(2) A-I, B-II, C-III, D-IV

(3) A-II, B-I, C-III, D-IV

(4) A-III, B-I, C-II, D-IV

Sol. **(A)**

(A) Intrinsic

(B) n-type semiconductor

(C) p-type semiconductor

(D) Metals

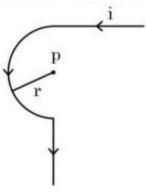
(II) Fermi-level in the middle of valence and conduction band

(III) Fermi-level near conduction band

(I) Fermi-level near valence band

(IV) Fermi-level inside the conduction band

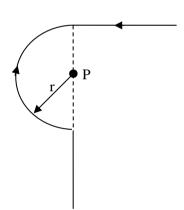
Find the magnetic field at the point P in figure. The curved portion is a semicircle connected to two 19. long straight wires.



 $(1)\frac{\mu_0 i}{2r} \left(1 + \frac{2}{\pi} \right) \qquad (2)\frac{\mu_0 i}{2r} \left(\frac{1}{2} + \frac{1}{2\pi} \right)$

 $(3)\frac{\mu_0 i}{2r} \left(1 + \frac{1}{\pi}\right)$ $(4)\frac{\mu_0 i}{2r} \left(\frac{1}{2} + \frac{1}{\pi}\right)$

Sol.



 $B_P = B_1 + B_2$ $=\frac{\mu_0 i}{4\pi r} + \frac{\mu_0 i}{4r}$

$$=\frac{\mu_0 i}{4r} \left[\frac{1}{\pi} + 1 \right]$$

$$B_{\rm P} = \frac{\mu_0 i}{2r} \left[\frac{1}{2\pi} + \frac{1}{2} \right]$$

The average kinetic energy of a molecule of the gas is 20.

(1) proportional to absolute temperature

(2) proportional to pressure

(3) proportional to volume

(4) dependent on the nature of the gas

Sol.

The average kinetic energy of gas molecule is given by,

 $K.E_{avg} = \frac{3}{2}KT$

 \therefore K.E_{avg} \propto T

SECTION - B

- A small particle moves to position $5\hat{i} 2\hat{j} + \hat{k}$ from its initial position $2\hat{i} + 3\hat{j} 4\hat{k}$ under the action of 21. force $5\hat{i} + 2\hat{j} + 7\hat{k}$ N. The value of work done will be ______ J.
- Sol.

$$\begin{split} & \Delta \vec{r} = \vec{r}_f - \vec{r}_i \\ &= \left(5\hat{i} - 2\hat{j} + \hat{k} \right) - \left(2\hat{i} + 3\hat{j} - 4\hat{k} \right) \\ & \overrightarrow{\Delta r} = 3\hat{i} - 5\hat{j} + 5\hat{k} \\ & \therefore W = \vec{F} \cdot \overrightarrow{\Delta r} \\ &= \left(5\hat{i} + 2\hat{j} + 7\hat{k} \right) \cdot \left(3\hat{i} - 5\hat{j} + 5\hat{k} \right) \\ &= 15 - 10 + 35 \\ &= 5 + 35 \end{split}$$

$$= (5\hat{i} + 2\hat{j} + 7\hat{k}) \cdot (3\hat{i} - 5\hat{j} + 5\hat{k}) \cdot (3\hat{i} - 5\hat{j} + 5\hat{k})$$

A certain pressure 'P' is applied to 1 litre of water and 2 litre of a liquid separately. Water gets 22. compressed to 0.01% whereas the liquid gets compressed to 0.03%. The ratio of Bulk modulus of water to that of the liquid is $\frac{3}{x}$.

The value of *x* is _____

Sol.

$$Bulk\ Modulus =\ V \frac{dP}{dV}$$

$$\frac{(B)_{\text{water}}}{(B)_{\text{liquid}}} = \frac{V \, dP / dV}{V \, dP / dV} = \frac{dP / 0.01}{dP / 0.03}$$

$$\therefore \frac{\left(B\right)_{water}}{\left(B\right)_{liquid}} = \frac{0.03}{0.01} = \frac{3}{1}$$

$$\frac{\left(\mathbf{B}\right)_{\text{water}}}{\left(\mathbf{B}\right)_{\text{liquid}}} = \frac{3}{1}$$

:. On comparing with $\frac{3}{x}$, The value of "x" will be "1'.

- A light of energy 12.75eV is incident on a hydrogen atom in its ground state. The atom absorbs the 23. radiation and reaches to one of its excited states. The angular momentum of the atom in the excited state is $\frac{x}{\pi} \times 10^{-17}$ eVs. The value of x is _____ (use $h = 4.14 \times 10^{-15}$ eVs, $c = 3 \times 10^8$ ms⁻¹).
- Sol.

The energy of electron in ground state = -13.6 eV

$$E_n - E_1 = 12.75$$

$$\therefore E_n = 12.75 - 13.6$$

$$E_n = -0.85$$

So "n" is given by

$$E_n = -\frac{13.6}{n^2}$$

$$n^2 = \frac{-13.6}{-0.85}$$

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$$n^{2} = 16 \Rightarrow \boxed{n = 4}$$

$$\Rightarrow L = \frac{nh}{2\pi} = \frac{x}{\pi} \times 10^{-17}$$

$$\Rightarrow 4 \times \frac{h}{2\pi} = \frac{x}{\pi} \times 10^{-17}$$

$$4 \times \frac{4.14 \times 10^{-15}}{2\pi} = \frac{x}{\pi} \times 10^{-17} \Rightarrow \frac{2 \times 4.14 \times 10^{-15}}{10^{-17}} = x$$

$$x = 8.28 \times 10^{2} \Rightarrow \boxed{x = 828}$$

- A charge particle of 2μ C accelerated by a potential difference of 100 V enters a region of uniform 24. magnetic field of magnitude 4mT at right angle to the direction of field. The charge particle completes semicircle of radius 3 cm inside magnetic field. The mass of the charge particle is $___$ × 10^{-18} kg.
- Sol. 144

$$R = \frac{mv}{qB} = \frac{p}{qB}$$

$$R = \frac{\sqrt{2mq\Delta V}}{qB}$$

$$R = \frac{}{qB}$$

$$3 \times 10^{-2} = \frac{\sqrt{2m \times 2 \times 10^{-6} \times 10^{2}}}{2 \times 10^{-6} \times 4 \times 10^{-3}}$$

$$2 \times 10^{-6} \times 4 \times 10^{-3}$$
$$3 \times 10^{-2} \times 2 \times 10^{-6} \times 4 \times 10^{-3} = \sqrt{4m \times 10^{-4}}$$

$$24 \times 10^{-11} = \sqrt{4m \times 10^{-4}}$$

$$m = \frac{24 \times 24 \times 10^{-22}}{4 \times 10^{-4}}$$

$$m = 144 \times 10^{-18} \text{ Kg}$$

- The amplitude of a particle executing SHM is 3 cm. The displacement at which its kinetic energy will 25. be 25% more than the potential energy is: _____ cm.
- Sol.

$$K.E = P.E + \frac{25}{100} \times P.E.$$

$$K.E = P.E + \frac{1}{4}P.E$$

$$K.E = \frac{5}{4}P.E$$

$$\frac{1}{2}K(A^2 - x^2) = \frac{5}{4} \times \frac{1}{2}Kx^2$$

$$4(A^2 - x^2) = 5x^2$$
$$4A^2 - 4x^2 = 5x^2$$

$$4A^2 - 4x^2 = 5x^2$$

$$9x^2 = 4A^2$$

$$x^2 = \frac{4}{9} \times (3)^2$$

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- 26. In an experiment to find emf of a cell using potentiometer, the length of null point for a cell of emf 1.5 V is found to be 60 cm. If this cell is replaced by another cell of emf E, the length-of null point increases by 40 cm. The value of E is $\frac{x}{10}V$. The value of x is ______.
- **Sol.** 25

$$E_1 = K\ell_1$$

$$E_2 = K\ell_2$$

$$\therefore \frac{\mathbf{E}_2}{\mathbf{E}_1} = \frac{\ell_2}{\ell_1}$$

$$\frac{E}{1.5} = \frac{100}{60}$$

$$\therefore E = 1.5 \times \frac{10}{6}$$

$$=\frac{3}{2}\times\frac{10}{6}$$

$$=\frac{5}{2}$$

$$= 2.5$$

$$=\frac{25}{10}$$

- A thin cylindrical rod of length 10 cm is placed horizontally on the principle axis of a concave mirror of focal length 20 cm. The rod is placed in a such a way that mid point of the rod is at 40 cm from the pole of mirror. The length of the image formed by the mirror will be $\frac{x}{3}$ cm. The value of x is _____.
- **Sol.** 32

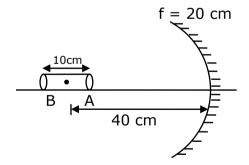


Image of end A:

$$u = -35$$
 cm

$$f = -20 \text{ cm}$$

$$v = ?$$

$$v = \frac{uf}{u - f}$$

$$= \frac{-35 \times -20}{-35 + 20}$$

$$=\frac{-35\times-20}{-15}$$

$$v = -\frac{140}{3}$$

Image of end B:

$$u = -45$$
 cm

$$v = ?$$

$$f = -20 \text{ cm}$$

$$v = \frac{uf}{u - f}$$

$$=\frac{-45 \times -20}{-45 + 20}$$

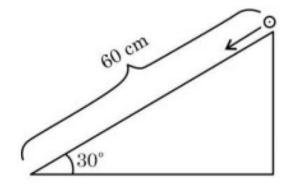
$$=\frac{-45\times-20}{-25}$$

$$v = -36$$

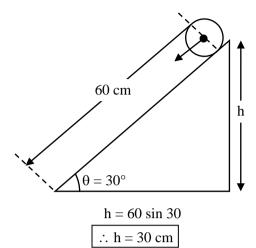
$$\therefore \text{ length of image} = \left| -36 + \frac{140}{3} \right|$$
$$= \left| -\frac{108 + 140}{3} \right|$$
$$= \frac{32}{3}$$

- \therefore The value of x = 32
- A solid cylinder is released from rest from the top of an inclined plane of inclination 30° and length 60 cm. If the cylinder rolls without slipping, its speed upon reaching the bottom of the inclined plane is _____ ms⁻¹.

 (Given $g = 10 \text{ ms}^{-2}$)



Sol.



The velocity of by linder upon reaching the ground is given by

$$V = \sqrt{\frac{2gh}{1 + \frac{K^2}{R^2}}}$$

$$\therefore V = \sqrt{\frac{2 \times 10 \times 30 \times 10^{-2}}{1 + \frac{1}{2}}}$$

$$= \sqrt{\frac{6 \times 2}{3}}$$

$$V = 2 \text{ m/s}$$

- A series LCR circuit is connected to an ac source of 220 V, 50 Hz. The circuit contain a resistance $R = 100\Omega$ and an inductor of inductive reactance $X_L = 79.6\Omega$. The capacitance of the capacitor needed to maximize the average rate at which energy is supplied will be _____ μ F.
- **Sol.** 40

For maximum power, the LCR must be in resonance.

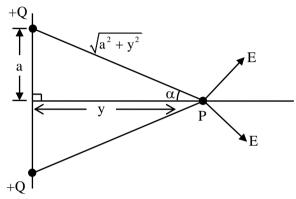
∴
$$X_L = X_C$$

 $79.6 = \frac{1}{\omega C}$
 $C = \frac{1}{\omega \times 79.6}$
 $= \frac{1}{2\pi \times 50 \times 79.6}$
 $= \frac{1}{100\pi \times 79.6}$
 $= 40 \times 10^{-6}$
 $= 40 \mu F$

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- **30.** Two equal positive point charges are separated by a distance 2a. The distance of a point from the centre of the line joining two charges on the equatorial line (perpendicular bisector) at which force experienced by a test charge q_0 becomes maximum is $\frac{a}{\sqrt{x}}$. The value of x is ______.
- Sol. 2



Electric field at point "P" due to any one change = $\frac{KQ}{a^2 + y^2}$

.. Net electric field at point "P" will be

$$E_{net} = 2E \cos \alpha$$

$$= \frac{2KQ}{a^2 + y^2} \times \frac{y}{\sqrt{a^2 + y^2}}$$

$$E_{net} = \frac{2KQy}{(a^2 + y^2)^{3/2}}$$

$$\Rightarrow$$
 Electric force (F) = $E_{net} q_0$

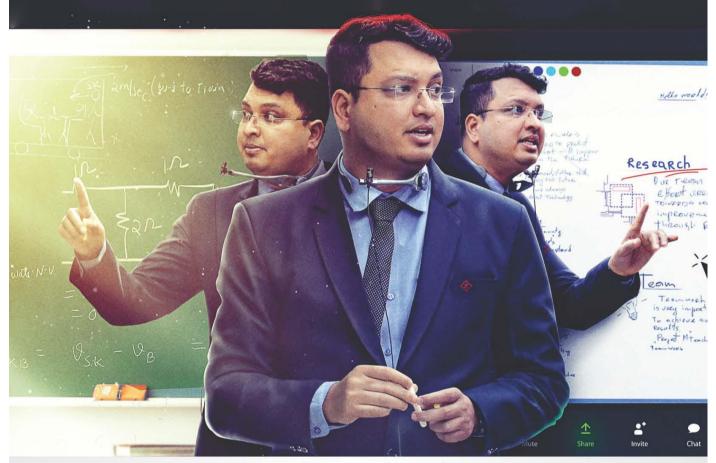
$$= \frac{2K \ Qq_0 y}{\left(a^2 + y^2\right)^{3/2}}$$

For
$$F = max \Rightarrow \frac{dF}{dy} = 0$$

By solving, we get
$$y = \frac{a}{\sqrt{2}}$$

$$\therefore$$
 the value of $x = 2$

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ADMISSION ANNOUNCEMENT

Session 2023-24 (English & हिन्दी Medium)

Target: JEE/NEET 2025 Hurture & प्रयास Batch

Class 10th to 11th Moving

Target: JEE/NEET 2024

Dropper & STATES Batch
Class 12th to 13th Moving

Target: JEE/NEET 2024
Enthuse & WATH Batch
Class 11th to 12th Moving

Target: PRE FOUNDATION
SIP, Evening & Tapasya Batch
Class 6th to 10th Students

